

Give the details of each characteristic for the following functions in problems (1) – (3)

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| a. Domain of the function   | f. Differentiability                         |
| b. $x$ - and $y$ -intercepts  | g. Intervals of increase and decrease        |
| c. Symmetry   | h. Local maximums and local minimums         |
| d. End behavior (limits at $\pm\infty$ ) including horizontal or slant asymptotes | i. Intervals of upward or downward concavity |
| e. Vertical Asymptotes  | j. Inflection points                         |

(1)  $f(x) = \frac{2(x^2-9)}{x^2-4}$

(2)  $f(x) = \frac{x}{\sqrt{x^2+2}}$

(3)  $f(x) = \frac{2x^3}{x^2+1}$

(4) Find two positive numbers such that the second is the reciprocal of the first and the sum is minimized.

(5) A box is to be made with a square base and no top. It must be made to hold 16 cubic inches of sand. Find the dimensions of the box of least surface area.